# Effective Programming Practices for Economists 

## Background

A Primer on Graphs

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## Graph definition

A graph $G$ is a pair $(N, E)$ of sets, where $N$ are nodes and $E$ are edges:

$$
G=(N, E)
$$

Edges are

- sets of two nodes (undirected graphs)
- pairs of nodes (directed graphs)

Chain (undirected)

$$
\begin{aligned}
N= & \left\{x_{0}, x_{1}, x_{2}, x_{3}\right\} \\
E=\{ & \\
& \left\{x_{0}, x_{1}\right\}, \\
& \left\{x_{1}, x_{2}\right\}, \\
& \left\{x_{2}, x_{3}\right\}
\end{aligned}
$$



Chain (undirected)

$$
\begin{aligned}
N= & \left\{x_{0}, x_{1}, x_{2}, x_{3}\right\} \\
E=\{ & \\
& \left\{x_{1}, x_{0}\right\}, \\
& \left\{x_{1}, x_{2}\right\}, \\
& \left\{x_{2}, x_{3}\right\}
\end{aligned}
$$



Chain (directed)

$$
\left.\begin{array}{rl}
N= & \left\{x_{0}, x_{1}, x_{2}, x_{3}\right\} \\
E= & \{ \\
& \left(x_{0}, x_{1}\right), \\
& \left(x_{1}, x_{2}\right), \\
& \left(x_{2}, x_{3}\right)
\end{array}\right\}
$$



Tree (undirected)

$$
\begin{aligned}
N= & \left\{x_{0}, x_{1}, \ldots, x_{8}\right\} \\
E= & \{ \\
& \left\{x_{0}, x_{1}\right\},\left\{x_{1}, x_{2}\right\},\left\{x_{2}, x_{3}\right\}, \\
& \left\{x_{2}, x_{4}\right\},\left\{x_{1}, x_{5}\right\},\left\{x_{5}, x_{6}\right\}, \\
& \left\{x_{5}, x_{7}\right\},\left\{x_{5}, x_{8}\right\} \\
\} &
\end{aligned}
$$



Tree (directed, "arborescence")

$$
\begin{aligned}
N= & \left\{x_{0}, x_{1}, \ldots, x_{8}\right\} \\
E=\{ & \\
& \left(x_{0}, x_{1}\right),\left(x_{1}, x_{2}\right),\left(x_{2}, x_{3}\right), \\
& \left(x_{2}, x_{4}\right),\left(x_{1}, x_{5}\right),\left(x_{5}, x_{6}\right), \\
& \left(x_{5}, x_{7}\right),\left(x_{5}, x_{8}\right)
\end{aligned}
$$



## Directed Acyclic Graph (DAG)

$$
\begin{aligned}
N= & \left\{x_{0}, x_{1}, \ldots, x_{8}\right\} \\
E= & \{ \\
& \left(x_{0}, x_{1}\right),\left(x_{1}, x_{2}\right),\left(x_{2}, x_{3}\right), \\
& \left(x_{2}, x_{4}\right),\left(x_{1}, x_{5}\right),\left(x_{5}, x_{6}\right), \\
& \left(x_{5}, x_{7}\right),\left(x_{5}, x_{8}\right),\left(x_{4}, x_{6}\right) \\
& \}
\end{aligned}
$$



## Directed Acyclic Graph

$$
\begin{aligned}
N= & \left\{x_{0}, x_{1}, \ldots, x_{8}\right\} \\
E=\{ & \\
& \left(x_{0}, x_{1}\right),\left(x_{1}, x_{2}\right),\left(x_{2}, x_{3}\right), \\
& \left(x_{2}, x_{4}\right),\left(x_{1}, x_{5}\right),\left(x_{5}, x_{6}\right), \\
& \left(x_{5}, x_{7}\right),\left(x_{5}, x_{8}\right),\left(x_{4}, x_{6}\right), \\
& \left(x_{5}, x_{0}\right) \\
\} &
\end{aligned}
$$



## Graph Use Cases

- The file system
- Git
- Reproducible research
- Causal theory
- Behavioural economics
- 

