Effective Programming Practices for Economists

Scientific Computing

Writing fast code with numpy

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Why numpy can be fast

- Numbers are stored efficiently in arrays
 - dtype of all numbers is known
 - it is fast to read numbers from memory into registers
- numpy functions are implemented very efficiently
 - in a low-level language like C
 - by experts who really know what they are doing
- Python overhead is incurred once per array, not once per number

Implications for writing fast code

- Vectorize everything!
- Use broadcasting where possible
- Prefer few large arrays over many small arrays

Why the example is slow

```
def array_cobb_douglas(factors, weights, a):
    out = np.empty(len(factors))
    for i in range(len(factors)):
         out[i] = _cobb_douglas(factors[i], weights, a)
    return out
def _cobb_douglas(factors, weights, a):
    return a * np.prod(factors**weights)
# (inputs as before)
%timeit array_cobb_douglas(factors, weights, a)
25.1 \text{ ms} \pm 488 \text{ } \mu \text{s} \text{ per loop}
```

- This uses array operations (e.g. np.prod) inside a loop
- This is typically slow and full vectorization should be faster
- Even writing out everything as a loop might be faster than the mix!

Full vectorization

```
def vectorized_array_cobb_douglas(factors, weights, a):
    return a * np.prod(factors**weights, axis=-1)
```

- From ~25 milliseconds to ~215 microseconds
- Speedup of more than 110×
- Code is actually more readable
- %timeit vectorized_array_cobb_douglas(factors, weights, a) \blacksquare 215 µs \pm 1.63 µs per loop
 - Need to get good with 'axis' argument!

Limits of performance with numpy

- Numpy is not a compiler, so it cannot
 - Fuse multiple operations into one (for more speed)
 - Eliminate intermediate results (for using less memory)
- Creating arrays is slower than creating list
 - Only relevant if you create many tiny arrays
- Calling array operations in a loop is typically slow but it is hard to detect this inefficiency in a profiler